

Policy on Reporting Uncertainties in Experimental Measurements & Results¹

$$Re = \frac{4}{\pi} \frac{\rho}{\mu} \frac{Q}{D} \quad (3)$$

Guidelines

An uncertainty analysis of experimental measurements is necessary for the results to be used to their fullest value. Authors submitting papers for publication to this Journal are expected to describe the uncertainties in their experimental measurements and in the results calculated from those measurements. The presentation of experimental data should include the following information:

- (1) The precision limit, P . The $\pm P$ interval about a result (single or averaged) is the experimenter's 95 percent confidence estimate of the band within which the mean of many such results would fall, if the experiment were repeated many times under the same conditions and using the same equipment. The precision limit is thus an estimate of the scatter (or lack of repeatability) caused by random errors and unsteadiness.
- (2) The bias limit, B . The bias limit is an estimate of the magnitude of the fixed, constant error. When the true bias error in a result is defined as β , the quantity B is the experimenter's 95 percent confidence estimate such that $|\beta| < B$.
- (3) The uncertainty U . The $\pm U$ interval about the result is the band within which the experimenter is 95 percent confident the true value of the result lies. The 95 percent confidence uncertainty is calculated from

$$U = [B^2 + P^2]^{1/2}$$

(1)

- (4) A brief description of, or reference to, the methods used for the uncertainty analysis. (If estimates are made at a confidence level other than 95 percent, adequate explanation of the techniques used must be provided.) The estimates of precision limits and bias limits should be made corresponding to a time interval appropriate to the experiment.

It is preferred that the following additional information also be included:

- (1) The precision limit and bias limits for the variables and parameters used in calculating each result.
- (2) A statement comparing the observed scatter in results on repeated trials (if performed) with the expected scatter ($\pm P$) based on the uncertainty analysis.

Although it is natural in any experimental paper to discuss sources of experimental error in the body of the text, this alone does not satisfy our requirement. All reported data must show uncertainty estimates. All tables should carry estimates. All figures reporting new data should contain uncertainty estimates either on the figure itself or in the caption.

A list of references on the topic, many of which appeared in the pages of this Journal is provided here in alphabetical order.

Example

Consider an experiment in which the pressure drop characteristics for fully developed flow conditions in a particular type of circular pipe are determined over a range of water flow rates. The outcome of this experiment might be presented by plotting one result—the Fanning friction factor, f , versus another result, the Reynolds number, Re . To obtain each "data point" that would be plotted on such a figure, the values of f and Re could be calculated from

$$f = \frac{\pi^2}{32} \frac{D^3}{\rho Q^2} \frac{(p_1 - p_2)}{(x_1 - x_2)} \quad (2)$$

and

where Q is the volumetric flow rate of the water with density ρ and dynamic viscosity μ . D the pipe diameter, p is the static pressure, x is axial position along the pipe, and the subscripts 1 and 2 refer to the upstream and downstream pressure tap locations, respectively.

The measured variables (Q , D , p_1 , p_2 , x_1 , x_2) and the parameters found from reference property data (ρ , μ) contain bias errors and precision errors. For example, calibrating pressure transducers under static conditions may later introduce bias errors if the measured field involves dynamic motions. Other bias errors arise from calibration of the measurement systems for p and Q against imperfect standards and from using property values originally determined in imperfect experiments. Precision errors could arise, for example, from sensitivity of the pressure transducer, flowmeter and data acquisition system to variations in ambient temperature and humidity. Inability to hold flow rate exactly constant during a period of data acquisition could also appear as a variation in the pressure measurements.

Errors in these quantities will propagate through Eqs. (2) and (3) to produce bias and precision errors in the results f and Re . The techniques of uncertainty analysis described in the references can be used to obtain estimates of the bias limits and precision limits for the variables and parameters and the bias limit, B , the precision limit, P , and the uncertainty, U , in the quantities f and Re .

If the two pressures, p_1 and p_2 are measured successively using the same absolute pressure transducer, the bias errors in the measurements of the two variables will not be independent of each other. This phenomenon of correlated bias errors occurs fairly often in the fluid and thermal sciences, usually when variables are measured using the same transducer or using different transducers that have been calibrated against the same standard. These effects must be taken into account in the uncertainty analysis. A method for doing this is shown in one example in ANSI/ASME PTC 19.1 and is derived and discussed in detail in Chapter 4 of Coleman and Steele [2].

References

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