

# The Role of Uncertainty Quantification in Verification and Validation of Computational Solid Mechanics Models

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AN INTERNATIONAL STANDARD



The American Society of  
Mechanical Engineers

**ASME VVUQ 10.2-2021**

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Two Park Avenue • New York, NY • 10016 USA

Date of Issuance: May 31, 2022

The next edition of this Standard is scheduled for publication in 2026.

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